Metasurface Optical Characterization Using Quadriwave Lateral Shearing Interferometry

Samira Khadir,* Daniel André, Ruggiero Verre, Qinghua Song, Serge Monneret, Patrice Genevet, Mikael Käll, and Guillaume Baffou*

ABSTRACT: An optical metasurface consists of a planar, dense distribution of scattering nanostructures with subwavelength sizes and interdistances behaving as a continuous and extremely thin optical component with predefined phase, transmission and reflection profiles. To date, various sorts of metasurfaces (metallic, dielectric, Huygens-like, Pancharatnam-Berry, etc.) have been introduced to design ultrathin lenses, beam deflectors, holograms, or polarizing interfaces. Their actual efficiencies depend on the ability to predict their optical properties and to fabricate nonuniform assemblies of billions of nanoscale structures on macroscopic surfaces. To further help improve the design of metasurfaces, precise and versatile postcharacterization techniques need to be developed. Today, most of the techniques used to characterize metasurfaces rely on light intensity measurements. Here, we demonstrate how quadriwave lateral shearing interferometry (QLSI), a quantitative phase microscopy technique, can achieve full optical characterization of metasurfaces of any kind, as it can probe the local phase imparted by a metasurface with high sensitivity and a spatial resolution that reaches the diffraction limit. As a means to illustrate the versatility of this technique, we present measurements on two types of metasurfaces, namely, Pancharatnam-Berry and effective-refractive-index metasurfaces, and present results on uniform metasurfaces, metalenses, and deflectors.

KEYWORDS: metasurface, metalens, quadriwave lateral shearing interferometry, quantitative phase imaging

An optical metasurface consists of a planar, dense distribution of scattering nanostructures with subwavelength sizes and interdistances behaving as a continuous and extremely thin optical component.1–3 By tailoring the distribution, composition, and morphology of the nanostructures, usually called meta-atoms or meta-units, the effective optical properties of the metasurface can be spatially adjusted to control the transmitted and reflected light in amplitude, phase, and polarization. In particular, in order to construct efficient phase optical elements, typically lenses, one has to design meta-units that can cover the full 0 → 2π phase-shift. This goal is impossible using meta-units consisting of single dipolar nanoparticles, the phase of which can only vary from 0 to π, since they behave as harmonic oscillators.4 Thus, more complex nanostructures have to be used, either consisting of thick structures (like pillars around 1 μm in height), to favor the occurrence of retardation effects and deviate from a dipolar response, or using Huygens-metasurfaces,5 based on shorter nanostructures that can reach a 2π phase shift when matching electric and magnetic dipole resonance frequencies. This past decade, many kinds of metasurfaces for different applications requiring flat optical components have been reported, such as metasurfaces to control reflection and refraction,6–8 focus light and control its polarization,9–11 produce a strong photonic spin Hall effect,12,13 and project holographic images.14,15

Designing a metasurface with a specific functionality usually relies on predictions obtained from numerical simulations, including basic effective index analysis,6 Huygens-metasurface designs,3 and more sophisticated optimization procedures.17–19 Novel and reliable optical characterization techniques would greatly facilitate a comparison between numerical predictions and actual metasurface measurements. Possible discrepancies and errors, originating either from the design or from fabrication imperfections, could be identified and compensated for to further improve device characteristics. To this end, several experimental characterization techniques have been utilized by the metasurface community, most of them relying on partial characterization or indirect measurements. Examples include measurements of polarization conversion efficiency, characterization of focal distance and
point-spread-function in the case of metalenses, and analysis of deflection angles for phase-gradient metasurfaces. In optics, however, the most natural method to measure phase is interferometry, typically based on two light beams (one used as a reference) recombined to interfere on a detection plane, as is done in ref to characterize plasmonic metasurfaces. Well-known drawbacks of the two-beam interferometry approach include noise and drift, leading to poor sensitivity, and complex setups that include two optical arms. To overcome these limitations, the three-beam method was proposed, where the third beam is used to analyze the environment and changes during an experiment, although this approach makes the setup even more complicated. Traditional ellipsometry has also been used to characterize metasurfaces. Although this characterization technique is much more accessible, it is restricted to the characterization of Pancharatnam-Berry (PB) metasurfaces. Then, the use of quasirefractive-index (ERI) and Pancharatnam-Berry (PB) metasurfaces, since it is simply based on the integration of a diffraction limit, constitutes a powerful tool to characterize the actual transformation applied by a metasurface on a light beam. Moreover, its implementation is much more straightforward than any other phase characterization techniques of metasurfaces, since it is simply based on the integration of a diffraction grating with a camera, which should favor its wide dissemination. The first part of the Article introduces the working principle of QLSI and the experimental configuration. In the second part, we introduce the two families of metasurfaces that will be investigated throughout the Article and that are commonly used for realizing efficient dielectric metasurfaces, namely, effective-refractive-index (ERI) and Pancharatnam-Berry (PB) metasurfaces. Then, the use of QLSI to characterize metasurfaces is exemplified first on uniform meta-atom distributions, to explain the principle and demonstrate the reliability of the technique, and then on two practical cases: beam defectors and metalenses.

### QUADRIWAVE LATERAL SHEARING INTERFEROMETRY (QLSI)

#### QLSI Working Principle

QLSI is a quantitative phase imaging technique based on the use of a wavefront analyzer composed of two simple elements: a regular camera and a two-dimensional diffraction grating, separated by a millimetric distance from each other. A good introduction to the working principle of QLSI can be found in ref. The diffraction grating (usually called a modified Hartmann mask, MHM) consists of a chessboard pattern of square transmitting

---

**Figure 1.** Working principle of QLSI. (a) Scheme of a QLSI microscope setup. A monochromator plasma source combined to a Köhler configuration illuminates the sample with a light beam controlled in wavelength, size, and numerical aperture. The light passing through the metasurface sample is collected by a microscope objective lens and sent to the QLSI wavefront analyzer, composed of a CMOS camera equipped with a modified Hartman mask (MHM). (b) Geometry of the modified Hartman Mask. (c) Schematic showing the wavefront distortion δ(x, y) experienced by a collimated light beam due to the presence of a metasurface.

---

https://dx.doi.org/10.1021/acsphotonics.0c01707

ACS Photonics 2021, 8, 603–613
units with alternating 0 and $\pi$ phase shifts (Figure 1b). This geometry cancels the 0 order and mainly produces first diffraction orders in four directions. The four diffraction orders create four slightly shifted images on the camera that interfere to create a so-called interferogram. The grating-camera distance is not crucial. The technique works over a large range of distances, usually in the millimetric range. The larger the distance, the better the sensitivity. The interferogram can be processed to retrieve both the intensity and the wavefront profiles $W(x, y)$ or, equivalently, the phase $\phi(x, y)$ of an incoming light beam. When mounted on a microscope, the measured wavefront profile is nothing but the optical path difference (OPD) image $\delta l(x, y)$ created by a sample in the object plane (Figure 1c). $\delta l = W$, and one usually defines

$$\delta l = \frac{\lambda_0}{2\pi} \phi$$

where $\lambda_0$ is the illumination wavelength and $\phi(x, y)$ is the phase delay experienced by a light beam crossing the sample in the object plane. The QLSI camera used in this study (Sid4 sc8 from Phasics S.A.) features an OPD sensitivity of 0.3 nm-Hz$^{-1/2}$ corresponding to around 3 mrad-Hz$^{-1/2}$ of phase delay in the visible range. Regarding the spatial (or lateral) resolution, it is limited by the diffraction limit associated with the numerical aperture of the objective lens, like in any optical microscopy technique. Importantly, QLSI benefits from the high sensitivity of interferometric methods but do not suffer from their usual drawbacks: it neither requires a reference beam, nor a complex alignment that might be sensitive to external perturbations. Compared with other existing interferometric techniques, this feature is what makes QLSI more accurate, reliable, and less likely to suffer from a signal that would come from illumination imperfection or instability. QLSI is a shot-noise limited technique. The relative positioning of the HMH with respect to the camera is done once and for all and is not sensitive to, for example, temperature variation, mechanical drift, or air flow. Most intensity and phase images presented in this study have been retrieved from interferogram images using a homemade algorithm. Over the past decade, several applications of QLSI have been demonstrated in biology and photonics, including cell imaging, temperature imaging in nano-plasmonics, 2D-material imaging, and single nanoparticle optical characterization. This work provides another application of QLSI for nanophotonics.

**Experimental Setup.** The experimental configuration of the optical microscope is depicted in Figure 1. The illumination part consists of a plasma laser-driven-light-source (EQ-99X from Energetiq Technologies) combined with a monochromator (Hypermonochromator, Mountain Photonics GmbH, purchased from Opton Laser International), enabling a variation of the wavelength over the visible range with a 6 nm bandwidth and a few mW of power. The use of an incoherent light source is preferable to avoid the appearance of fringes and speckles on the images. The optical fiber from the monochromator was positioned in a Köhler optical scheme to illuminate the sample with a sufficient degree of spatial coherence. This caution is a requirement in QLSI to achieve interferometric measurements despite the incoherent nature of the light source.
the light source. In all the measurements, we used a 40X Olympus objective (LUCPLFLN40X), with a tube lens of focal distance 200 mm (magnification: 44×), except for the uniform metasurface characterization, where we used a 40X Nikon (S Fluor 40X), f = 200 mm, (magnification: 40×). The light passing through the sample is imaged by the microscope on the QLSI wavefront analyzer. Each measurement requires the acquisition of a reference image over a clear area (without any object) prior to taking an image with the object of interest within the field of view (in our case a metasurface). The reference is then subtracted from the object image to discard any imperfections of the incoming light beam. In the specific case of Pancharatnam-Berry metasurfaces characterization, a set of two optical polarizers and two quarter waveplates are added to the setup to study the device response in the standard circular cross-polarization configuration. We used a MHM provided by the Phasics company, implemented on a Zyla 5.5 camera (Andor, Si4-sC8, Phasics).

**Metasurfaces Principles and Designs.** As a means to demonstrate the versatility of QLSI for metasurfaces characterization, two opposite families of metasurfaces have been investigated, namely, effective-refractive-index metasurfaces (Figure 2a), where the transmitted phase depends on the size of the meta-units, and Pancharatnam-Berry metasurfaces (Figure 2b), where the phase depends on the orientation of the meta-units.

**Effective-Refractive-Index Metasurfaces.** Effective-refractive-index (ERI) metasurfaces are often composed of a dense distribution of cylindrical pillars operating as independent Fabry–Perot resonators with a low quality factor (Figure 2a). The pillars are sufficiently tall to accommodate internal multilongitudinal-mode propagation, but remains sufficiently narrow to achieve large pillar density and prevent propagation of nonzero diffraction orders in free space or in the substrate.39 The resulting effective refractive index of the pillar layer and, thus, the phase delay can be adjusted by varying the pillar diameter. In this study, we used a periodic square array of nanopillars made of GaN (see Figure 2b and Materials and Methods), 1 μm in height and with a 300 nm pitch, with diameters varying from 114 to 206 nm (see Figure 2c).

**Pancharatnam-Berry Metasurfaces.** The Pancharatnam-Berry (PB) phase is a kind of geometrical phase acquired by a light beam when passing through a birefringent medium.40 PB metasurfaces are composed of asymmetric meta-units usually consisting of dielectric nanofins and providing the metasurface with birefringent properties (Figure 2b).20,41,42 To achieve maximum efficiency, PB metasurfaces require the use of circularly polarized illumination and detection of the circularly polarized light with the opposite handedness (see linear polarizers and quarter waveplates in Figure 1). Thus, in this cross-polarization configuration, no light is supposed to be detected, except where the sample features some birefringence, that is, where PB meta-units are present. The action of the nanofin on a light beam can be simply modeled assuming the nanofins act as a polarizing plate associated with the following Jones matrix:

**Figure 3.** QLSI characterization of uniform metasurfaces. (a) Phase and (b) intensity images of 12 circular arrays (30 μm in diameter) of different GaN nanopillars, the sizes of which increase gradually from left to right and then from top to bottom. The targeted phase values are indicated on the phase image for each area, varying by steps of 30°. (c) Measurements of the phase and normalized intensity of the circular metasurfaces shown in images (a) and (b). (d) Phase and (e) intensity images of 12 circular arrays (30 μm in diameter) of different polymer nanofins, the orientation of which varies gradually by steps of 15° to make the phase vary by steps of 30°. The targeted phase values are indicated on the phase image for each area. (f) Measurements of the phase and normalized intensity of the circular metasurfaces shown in images (d) and (e).
Effective-Refractive-index metasurface

\[ \Gamma(\beta) = \begin{pmatrix} e^{\beta/2} & 0 \\ 0 & e^{-\beta/2} \end{pmatrix} \]

where \( \beta \) characterizes the meta-atom anisotropy. In this case, the complex amplitude \( A \) of the detected light in the circular cross-polarized configuration is given by (see derivation in Supporting Information):

\[ A(\theta) = ie^{i\theta} \sin(\beta/2) \]

where \( \theta \) is the angle of the nanofin and \( \sin(\beta/2) \) is called the conversion efficiency. As expected, for nonbirefringent structures (\( \beta = 0 \)), no light is detected (\( A = 0 \)) due to the crossed polarization configuration in illumination and detection. The value of \( \beta \) depends on the morphology, which can be optimized at a given wavelength to approach as much as possible \( \sin(\beta/2) = 1 \), that is, \( \beta = \pi \), which means that an ideal PB meta-unit should act as a half-wave plate (\( \Gamma(\pi) \)). In this study, we used nanofins made of a patterning polymer with a pitch of 500 nm (see Figure 2d–f and Materials and Methods).

The transmission of light with the opposite handedness is due to the presence of birefringent structures, and eq 3 indicates that the phase of this transmitted light is dictated by the orientation of the nanofins. Setting the nanofin angle to \( \theta \) results in a change of the local geometric phase of \( 2\theta \), no matter the composition or the morphology of the nanofin, providing it has some anisotropy.

The phase of ERI and PB meta-units are adjusted by varying, respectively, their size and their angle. In most nanofabrication techniques, a diameter is more difficult to accurately control compared to an angle. For instance, different e-beam doses are markedly affecting the sizes of lithographically fabricated objects, but not their orientations. For this reason, ERI metasurfaces are particularly sensitive to nanofabrication inaccuracies. Any inaccuracy in the PB meta-atom size only affects the conversion efficiency (\( \sin(\beta/2) \) in eq 3), that is, the transmitted intensity, not the phase shift. Here lies the benefit of PB metasurfaces. PB metasurfaces are also dispersiveless (i.e., achromatic) since the phase of \( A(\theta) \) (eq 3) is wavelength-independent, unlike ERI metasurfaces. However, PB metasurfaces are not outperforming ERI metasurfaces in any aspect. The main limitation of PB metasurfaces is the necessity to work with circularly polarized light to achieve maximum efficiency. In the following, we illustrate and discuss the use of QLSI for these two families of metasurfaces.

## RESULTS

Characterization of Uniform Metasurfaces. Figure 3 presents QLSI images of uniform metasurfaces. In both case studies (ERI and PB), 12 circular “phase-piston” metasurfaces have been imaged within a single field of view. Each metasurface corresponds to a given phase shift, varying gradually by steps of 30° to span the entire 2π range.

The case of ERI metasurfaces corresponds to Figure 3a–c. The phase shifts are uniform over each disc, and the values are reported in Figure 3c. The agreement with the targeted phase is very good, except for phase shifts close to \( \pi \). This issue is expected: QLSI primarily measures phase gradient images over \( x \) and \( y \) directions. The phase image is subsequently reconstructed numerically from these two gradient images. When a phase jump close to \( \pi \) occurs between neighboring pixels in a gradient image, the phase reconstruction algorithm cannot really know if the phase is actually decreasing or increasing and may assign a phase gradient of \( \pm \pi \), the sign of which is highly noise-dependent. This random sign attribution can create some rendering issues, such as discontinuities and singularities in the phase image, like in the top-left area of Figure 3a. However, this issue is not expected to occur for most metasurface characterizations, as metasurfaces rarely exhibit phase steps of \( \pi \) and generally rather consist of regular and smooth variations of phase over space (see the metasurfaces and metagradient characterization hereinafter). This \( \pi \) phase...
A step issue with QLSI has never been the subject of any particular study, as it rarely causes a problem: Objects typically studied by QLSI are usually smooth in phase, without phase discontinuities. We are not aware of alternative retrieval algorithms that could solve the problem. Nevertheless, this issue is certainly worthy of future attention since an improved phase retrieval algorithm able to deal with this current limitation would not only allow a more efficient characterization of metasurfaces, but also advance the QLSI technique in itself. Finally, QLSI also enables the reconstruction of the intensity image from the interferogram image. The normalized intensity image is displayed in Figure 3b, and measurements are reported in Figure 3c, which have to be compared with Figure 2c. This transmission of the metasurfaces is close to the theoretical prediction (Figure 2c.), that is, quite constant upon varying the nanopillar diameter.

The case study of PB uniform metasurfaces is presented in Figures 3d−f. The sample contained 12 uniform and circular metasurfaces, in which the nanoﬁn angle varied from one metasurface to another by increments of 15° to generate phase increments of 30° and cover the full 2π phase-shift. The circular areas observed in the images were surrounded by a uniform sea of nanoﬁns oriented as in the 0° area, as a means to get nonzero light intensity outside the circular areas and also to have a nearby blank area with some transmitted light to acquire the reference image. The absence of a layer of PB meta-units around the metasurface would have resulted in a zero light intensity background, which is likely to create large noise on the image and even rendering issues upon reconstruction of the phase image. The phase values are reported in Figure 3f, with a good agreement with theory, except, again, when the phase is close to π, for the reason mentioned above. The normalized intensity image is displayed in Figure 3e and measurements are reported in Figure 3f, which have to be compared with Figure 2f. The transmission of the metasurfaces is not as uniform as expected upon varying the nanoﬁn angle. This discrepancy can result from a near-ﬁeld interaction between neighboring nanoﬁns or possibly from some misalignment of the illumination and detection polarizing plates.

Characterization of Beam Defectors. We now focus the study on a textbook case that is a beam deﬂecting or beam steering metasurface.6,23,43,44 Again, we studied deﬂectors made of both ERI and PB metasurfaces. The devices have been designed to deﬂect light on the air side at a ﬁxed angle of θ = 5°. Considering (Oy) as the direction of deﬂection, the theoretical OPD reads

$$\delta l(y) = yn \sin(\theta)$$

where n is the refractive index of the medium (n = 1 in our case).

Experimental results are presented in Figure 4. SEM images (Figure 4a,e) detail gradual distribution of meta-units at the nanoscale. OPD images (Figure 4b,f) display the expected linear gradient of phase, in very good agreement with theory (Figures 4d,h). No ﬁtting parameter has been introduced, except an arbitrary OPD offset. Also, no nanostructuration/roughness is included in the theoretical curve, which is only a linear function. Intensity images (Figure 4c,g) display some nonuniformities but do not noticeably affect the phase gradient.

Figure 5. QLSI characterization of metalenses. (a) OPD images of the ERI metalens recorded by QLSI, along with its (b) radially averaged proﬁle. (c) Normalized intensity image recorded by QLSI, associated with image (a), along with its (d) radially averaged proﬁle. (e−h) Same as (a−d), for the PB metalens illuminated by a left-handed circular polarization (LHCP) beam. (i−l) Same as (e−h), the PB metalens illuminated by a RHCP beam. Scale bars for QLSI images: 50 μm.
Characterization of Metalenses. We focus now on the most common application of a metasurface, which is the metalens. We studied equivalent ERI and PB metalenses, designed with a fixed radius of \( R = 100 \, \mu m \) and a focal length of \( f = 500 \, \mu m \) (NA \( \sim 0.2 \)). The theoretical OPD profile of such lenses is given by

\[
\delta l(r) = \mp \sqrt{(r^2 + f^2)} + C \tag{5}
\]

where \( r \) is a radial coordinate and \( C \) is a constant. The signs “-“ or “+“ correspond to convergent or divergent metalenses, respectively.

Figure S5a-d presents results on the characterization of an ERI metalens using QLSI. The radially averaged OPD profile (Figure S5b) shows a perfect agreement with theory (see eq 5). In all the numerical plots of Figure S5, no fitting parameter has been used, except the offset \( C \) in eq 5. The intensity profile (Figure S5d) is not perfectly uniform, exhibiting spatial variations in agreement with Figure 3c.

Figure S5e-l presents results on the characterization of a PB metalens. Again, phase measurements (Figure S5e) perfectly match theoretical predictions (Figure S5f). Interestingly, for PB metalenses, reversing the handedness of both the illumination and detection circular polarizations leads to a metalens with the opposite focal length \( -f \). This effect is indeed observed and characterized in Figure S1i, which reproduces the theoretical predictions (Figure 5j). Just like with the ERI metalens, unexpected features are observed in the transmission profiles (Figure S5h,i): While theory predicts a transmission that is independent of the \( f \) orientation (see eq 3), variations are observed throughout the metalens in agreement with Figure 3f. We evidence here that this nonuniform transmittance does not affect the quality of the phase profile.

Measurements of Zernike moments is common to characterize the aberrations of an optical system with circular pupils.\(^{45,46}\) We explain hereinafter how QLSI can efficiently measure Zernike moments of metasurfaces. The Zernike polynomials \( Z_m^n \) are defined over the unit disk \( r \in [0, 1], \phi \in [0, 2\pi] \) as

\[
Z_m^n(r, \theta) = R_m^n(r)e^{i\theta} \tag{6}
\]

\( n \) and \( m \) are integers, following the restrictions \( n \geq 0, 0 \leq m \leq n \), and \( m \) of the same parity as \( n \). \( R_m^n(r) \) are polynomials with real coefficients, called the radial Zernike polynomials. For instance, \( R_1^0(r) = r, R_2^0(r) = 2r^2 - 1 \), and \( R_2^1(r) = r^2 \). Any smooth, real function \( F \) defined over a disc can be written as a linear combination of Zernike polynomials \( \{Z_m^n\}_{n,m \in N} \), which form an orthonormal image basis:

\[
F = \frac{1}{2} \sum_{n,m} c_{n,m}Z_m^n + c_{n,m}Z_n^m \tag{7}
\]

\( c_{n,m} \) are complex coefficients called the complex Zernike moments of the image. The first elements of the Zernike basis, corresponding to the lowest spatial frequencies of the image, are represented in Figure 6a. Calculation of the moments of an image, such as the phase image represented in Figure S5a,g,i, requires to precisely define the center and the radius of the disc over which the moments have to be calculated. Then, the Zernike moments can be retrieved using

\[
c_{n,m} = \frac{2(n + 1)}{\pi \epsilon_m} \int_0^1 \int_0^{2\pi} F(r, \phi)Z_m^n(r, \phi)r \, dr \, d\phi \tag{8}
\]

where \( \epsilon_m = 2 \) for even \( m \) values and \( \epsilon_m = 1 \) for odd \( m \) values: \( \epsilon_m = 2 - \text{modulo}(m, 2) \). \( Z_1^0(r, \phi) = r \) represents a tilt over the direction \( \phi \). This moment is particular and requires some comments. First, the moment does not depend on the center of the disc on which the moment is calculated, contrary to all the other moments. Second, this moment is not really important for the characterization of the metalens as it affects neither the point

![Figure 6. QLSI and Zernike analysis of metalenses. (a) Numerical simulations of the real parts of Zernike polynomials up to \( n = 5 \). (b) (Left) Optical thickness of an ERI metalens, from which the Zernike mode \( Z_0^2 \) was subtracted, highlighting the lens aberrations and imperfections. (Right) Measurements of the Zernike moments up to \( n = 5 \). (c) (Left) Optical thickness of a PB metalens from which the Zernike mode \( Z_0^2 \) was subtracted. (Right) Measurements of the Zernike moments up to \( n = 5 \). (d) Same as (c) for the opposite circularly polarized illumination handedness.](https://dx.doi.org/10.1021/acsphotonics.0c01707)
metalens aberrations. This rule applies any time the polar-beam and the metalens and cannot be only attributed to reference image may not compensate for this problem. Thus, result in additional phase nonuniformity. The acquisition of a dependence on the light beam quality: any nonuniform deviation metasurfaces is here that the Zernike moments can also rotating the circular polarizations. The di

\[ f = -\frac{R_2^2}{4c_{2,0}} \]  

Figure 6c,d addresses the case of a PB metalens, used as a convergent (Figure 6c) or divergent (Figure 6d) lens by rotating the circular polarizations. The difference with ERI metasurfaces is here that the Zernike moments can also depend on the light beam quality: any nonuniform deviation from a perfect circular polarization over the field of view may result in additional phase nonuniformity. The acquisition of a reference image may not compensate for this problem. Thus, the measured Zernike moments characterize both the light beam and the metalens and cannot be only attributed to metalens aberrations. This rule applies any time the polar-

Figure 7. QLSI measurements of light propagation after a PB metalens. (a, b) LHCP/RHCP and (b, c) RHCP/LHCP configurations: (a) and (c) are intensity measurements and (b) and (d) are OPD measurements.

ization (linear or circular) matters for the characterization of metalenses, but can be more problematic for PB metasurfaces because perfectly circular polarizations are more complicated to achieve compared with linear polarizations. Any QLSI experiment on PB metasurfaces investigating high-order Zernike coefficients has to carefully set the circular polarizations in illumination and detection in order to faithfully probe the metalens quality and not something else. If a doubt regarding the beam quality persists, we recommend characterizing the metasurface at different positions within the field of view of the microscope by moving the sample holder to acquire one image in each quadrant, for instance. If the measured aberrations remain the same, then they are an intrinsic characteristic of the beam. If the aberrations are position-dependent, then the polarization uniformity of the beam has to be improved.

QLSI imaging is not limited to the focus plane. The technique can image the phase profile anywhere in space. In particular, QLSI can also characterize the light propagation in phase and intensity after crossing the metasurface as a means to better characterize the action of a metasurface. For this purpose, we translated the objective lens along its optical axis (Oz) and acquired several images as a function of its position along Oz. An equivalent option could have been to translate the sample along Oz. The intensity image presented in Figure 7a confirms that the light beam exiting the metalens is focused at a distance that corresponds to the focal length (f = 500 μm). The OPD distribution (Figure 7b) exhibits an inversion of the contrast at the focal point corresponding to a phase shift of π. This phenomenon is known as the Gouy phase shift. The tiny instabilities of the OPD image close to the focus spot, observed in Figure 7b, result from the lack of spatial coherence: At the location of the focus spot, the metalens images the source, which is in our experiment the exit of the optical fiber of the monochromator that is not spatially coherent. QLSI performs less well in this condition. In practice, the image of the light source should be sent to infinity and not imaged. Figure 7c,d reports measurements using the

\[ Z_2^0(r, \phi) = 2r^2 - 1 \]  

The second polynomial that requires attention, especially for a metalens, is \( Z_2^0(r, \phi) = 2r^2 - 1 \). When applied to an image obtained with an imaging system, \( Z_2^0 \) normally corresponds to the aberation called defocus. But when characterizing a lens, it is nothing but the moment corresponding to the phase profile of the lens itself, at least at the first order. Besides, the focal length of the metalens is linked to the \( Z_2^0 \) moment by the expression (see derivation in Supporting Information):

\[ f = -\frac{R_2^2}{4c_{2,0}} \]
reverse circular polarization configuration, where the metalens acts as a divergent lens. Regarding the light intensity (Figure 7c), it is vanishing upon propagation due to the divergence of the beam, with a residual, weak converging beam (1 order of magnitude lower than for the convergent lens) due to some imperfection of the illumination leading to a leakage of copolarized light. Regarding the phase profile (Figure 7d), the region 0–100 μm away from the metasurface clearly exhibits a diverging behavior, as the phase profile is convex and spreading out.

■ CONCLUSION

We have demonstrated how quadriwave lateral shearing interferometry (QLSI) can fully characterize the optical properties of metasurfaces in a simple, versatile, and accurate way. To illustrate the versatility of QLSI for metasurface metrology, we presented measurements on effective-refractive-index and Pancharatman-Berry metasurfaces. We highlighted the benefits of the techniques, but also the limitations, in particular, when dealing with local π phase steps. We also introduced the possibility and tested the capability of QLSI to measure metasurface imperfections using a Zernike polynomial approach. For the sake of clarity and conciseness, all the results presented in this study were restricted to the particular wavelength for which the metasurfaces were designed. However, nothing prevents one from performing measurements at other wavelengths, for instance, to quantify chromatic imperfections of sin(β/2) ≈ 50% at the operating wavelength of 530 nm. Using this type of metasurface building block, a hyperbolic lens with a focal length of 500 μm as well as a linear phase gradient metasurface were built. In the case of uniform metasurfaces and defectors (but not in the case of metalenses), the metasurfaces were surrounded by a uniform sea of fins as a means to have light transmission also around the metasurfaces. All PB metasurfaces have been designed to be used at a wavelength of 532 nm.

PB Metasurface Fabrication. We fabricated the PB metasurfaces using a novel approach based on the use of a patternable polymer (ma-N 2410, Micro Resist Technology GmbH, Germany) as the metasurface building material itself. The fabrication process is described in detail in ref 48. This fabrication technique allows for a facile route to make large-scale, high efficiency gradient metasurfaces. The constituent meta-units are freestanding nanofins with the dimension 400 × 140 × 1700 nm (Figure 2), which when placed in a square lattice with a 500 nm period, present a polarization conversion efficiency of sin(β/2) ≈ 50% at the operating wavelength of 530 nm. Using this type of metasurface building block, a hyperbolic lens with a focal length of 500 μm as well as a linear phase gradient metasurface were built. In the case of uniform metasurfaces and defectors (but not in the case of metalenses), the metasurfaces were surrounded by a uniform sea of fins as a means to have light transmission also around the metasurfaces. All PB metasurfaces have been designed to be used at a wavelength of 532 nm.

■ MATERIALS AND METHODS

ERI Metasurface Fabrication. Effective-refractive-index metasurfaces were made of square periodic arrays of GaN pillars, 1 μm in height, 300 nm pitch. They have been revealed by patterning a 1 μm thick GaN layer grown on a double-sided polished c-plane sapphire substrate using a Molecular Beam Epitaxy (MBE) RIBER system. Conventional electron beam lithography (EBL) was used to expose a double layer of ~200 nm PMMA resist (495AA) spin-coated on the GaN thin-film and then baked on a hot plate at 125 °C. E-beam resist exposure was then performed at 20 keV (using a Raith ElphyPlus, Zeiss Supra 40), followed by PMMA development using a 3:1 IPA:MIBK solution. After development, a 50 nm layer of Ni was deposited using e-beam evaporation to perform a metallic film liftoff by immersing the sample into acetone solution for 2 h. The resulting Ni pattern was utilized as a hard mask during the reactive ion etching (RIE, Oxford system with a plasma composed of Cl₂, CH₂, Ar gases, with flows of 13, 2, and 2 sccm, respectively) to transfer the pattern in the GaN layer. Finally, the Ni hard mask on the top of GaN nanopillars was removed using chemical etching with a 1:2 HCl/HNO₃ solution. ERI metasurfaces have been designed to be used at a wavelength of 600 nm.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsphotonics.0c01707.

Complex transmittance for PB metasurface (eq 3) and a demonstration of the relation between the focal length of a metalens and the εg0 Zernike moment of its phase image (eq 9) (PDF)

■ AUTHOR INFORMATION

Corresponding Authors
Samira Khadir – Université Côte d’Azur, CNRS, CRHEA, Sophia Antipolis 06560, Valbonne, France; Institut Fresnel, CNRS, Aix Marseille University, Marseille 13013, France; orcid.org/0000-0002-2280-4099; Email: samira.khadir@crhea.cnrs.fr
Guillaume Baffou – Institut Fresnel, CNRS, Aix Marseille University, Marseille 13013, France; orcid.org/0000-0003-0488-1362; Email: guillaume.baffou@fresnel.fr
Complete contact information is available at: https://pubs.acs.org/10.1021/acsphotonics.0c01707

Notes
The authors declare no competing financial interest.

■ ACKNOWLEDGMENTS

S.K., Q.S., and P.G. acknowledge financial support from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme (Grant Agreement FLATLIGHT No. 639109 and Grant Agreement i-LiDAR No. 874986), and from the French government, through the UCAJEDI Investments in the Future project managed by the National Research Agency (ANR) with the reference number ANR-15-IDEX-01. D.A., R.V., and M.K. would like to thank the Knut and Alice Wallenberg Foundation, the Swedish Foundation for Foundation for Strategic Research and the Excellence Initiative Nano at Chalmers University of Technology. This work was partially performed at Myfab Chalmers. The authors thank B. Wattellier and R. Laberdesque for helpful discussions.

■ REFERENCES


